2012-DSE MATH CP PAPER 2

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2012

# MATHEMATICS Compulsory Part PAPER 2

 $11.30 \text{ am} - 12.45 \text{ pm} (1\frac{1}{4} \text{ hours})$ 

#### INSTRUCTIONS

- 1. Read carefully the instructions on the Answer Sheet. After the announcement of the start of the examination, you should first stick a barcode label and insert the information required in the spaces provided. No extra time will be given for sticking on the barcode label after the 'Time is up' announcement.
- When told to open this book, you should check that all the questions are there. Look for the words 'END OF PAPER' after the last question.
- 3. All questions carry equal marks.
- 4. **ANSWER ALL QUESTIONS**. You are advised to use an HB pencil to mark all the answers on the Answer Sheet, so that wrong marks can be completely erased with a clean rubber. You must mark the answers clearly; otherwise you will lose marks if the answers cannot be captured.
- 5. You should mark only ONE answer for each question. If you mark more than one answer, you will receive NO MARKS for that question.
- 6. No marks will be deducted for wrong answers.

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Not to be taken away before the end of the examination session

There are 30 questions in Section A and 15 questions in Section B. The diagrams in this paper are not necessarily drawn to scale. Choose the best answer for each question.

## Section A

1. 
$$\frac{(2x^4)^3}{2x^5} =$$

- A.  $3x^2$ .
- B.  $3x^{7}$ .
- C.  $4x^7$ .

  D.  $4x^{59}$ .

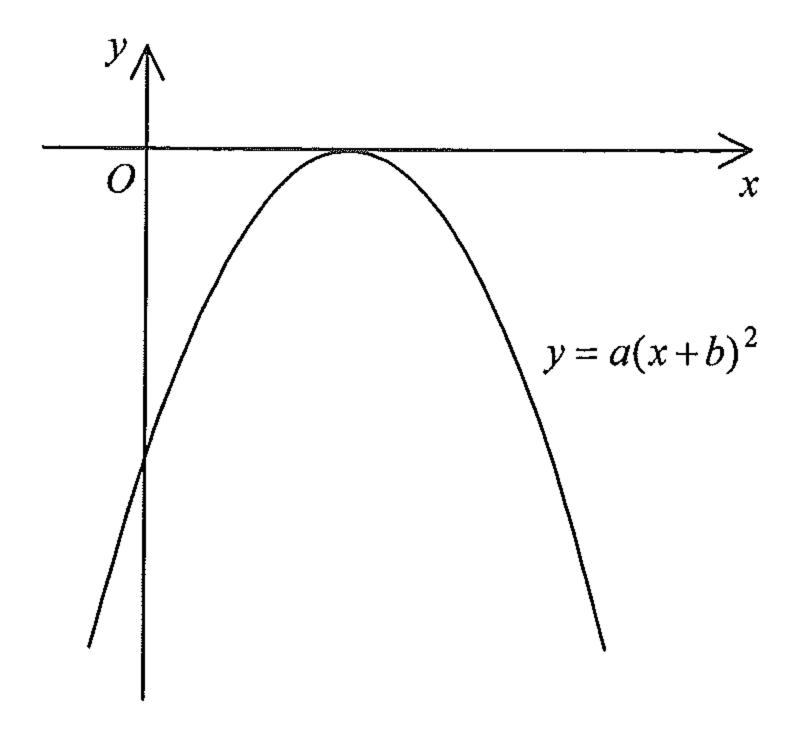
2. 
$$(4x+y)^2-(4x-y)^2=$$

- B.  $2y^2$ .
- 8xy.
- D. 16xy.

3. If p and q are constants such that 
$$x^2 + p = (x+2)(x+q)+10$$
, then  $p =$ 

- B.
- 6.
- 10. D.

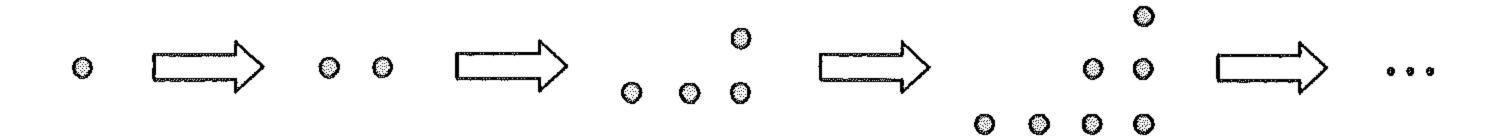
- 4. If k is a constant such that  $x^3 + 4x^2 + kx 12$  is divisible by x + 3, then k =
  - A. -25.
  - B. -1.
  - C. 1.
  - D. 17.
- 5. If m+2n+6=2m-n=7, then n=
  - A. -4.
  - B. -1
  - C. 3.
  - D. 11.
- 6. The figure shows the graph of  $y = a(x+b)^2$ , where a and b are constants. Which of the following is true?
  - A. a > 0 and b > 0
  - B. a > 0 and b < 0
  - C. a < 0 and b > 0
  - D. a < 0 and b < 0



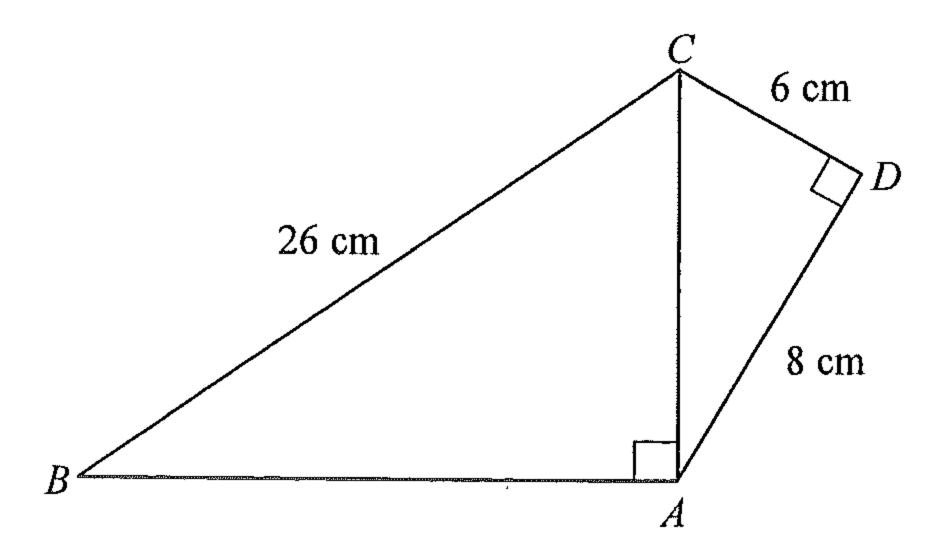
- 7. The solution of 15+4x<3 or 9-2x>1 is
  - A. x < -3.
  - B. x > -3.
  - C. x < 4.
  - D. x > 4.

- 8. In a company, 37.5% of the employees are female. If 60% of the male employees and 80% of the female employees are married, then the percentage of married employees in the company is
  - A. 32.5%.
  - B. 45%.
  - C. 55%.
  - D. 67.5%.
- 9. If x and y are non-zero numbers such that  $\frac{6x+5y}{3y-2x} = 7$ , then x: y =
  - A. 4:5
  - B. 4:13.
  - C. 5:4.
  - D. 13:4.
- 10. It is given that y partly varies directly as  $x^2$  and partly varies inversely as x. When x = 1, y = -4 and when x = 2, y = 5. When x = -2, y =
  - A. -11.
  - В. –5.
  - C. 5.
  - D. 11.
- 11. Mary performs a typing task for 7 hours. Her average typing speeds for the first 3 hours and the last 4 hours are 63 words per minute and 56 words per minute respectively. Find her average typing speed for the 7 hours.
  - A. 17 words per minute
  - B. 35 words per minute
  - C. 59 words per minute
  - D. 60 words per minute

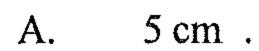
12. In the figure, the 1st pattern consists of 1 dot. For any positive integer n, the (n+1) th pattern is formed by adding n dots to the nth pattern. Find the number of dots in the 8th pattern.



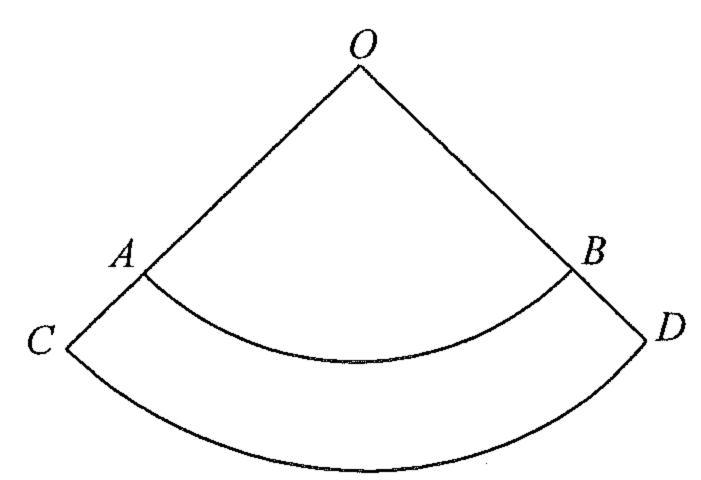
- A. 22
- B. 29
- C. 36
- D. 37
- 13. 0.0322515 =
  - A. 0.032 (correct to 3 significant figures).
  - B. 0.0322 (correct to 4 decimal places).
  - C. 0.03225 (correct to 5 significant figures).
  - D. 0.032252 (correct to 6 decimal places).
- 14. The length of a piece of thin string is measured as  $25 \,\mathrm{m}$  correct to the nearest  $\,\mathrm{m}$ . If the string is cut into n pieces such that the length of each piece is measured as  $5 \,\mathrm{cm}$  correct to the nearest  $\,\mathrm{cm}$ , find the greatest possible value of n.
  - A. 445
  - B. 566
  - C. 567
  - D. 650
- 15. In the figure, the area of quadrilateral ABCD is
  - A.  $144 \text{ cm}^2$ .
  - B.  $160 \text{ cm}^2$ .
  - C.  $178 \text{ cm}^2$ .
  - D.  $288 \text{ cm}^2$ .



16. In the figure, OAB and OCD are sectors with centre O. If  $\widehat{AB} = 12\pi \, \mathrm{cm}$ ,  $\widehat{CD} = 16\pi \, \mathrm{cm}$  and  $OA = 30 \, \mathrm{cm}$ , then AC =





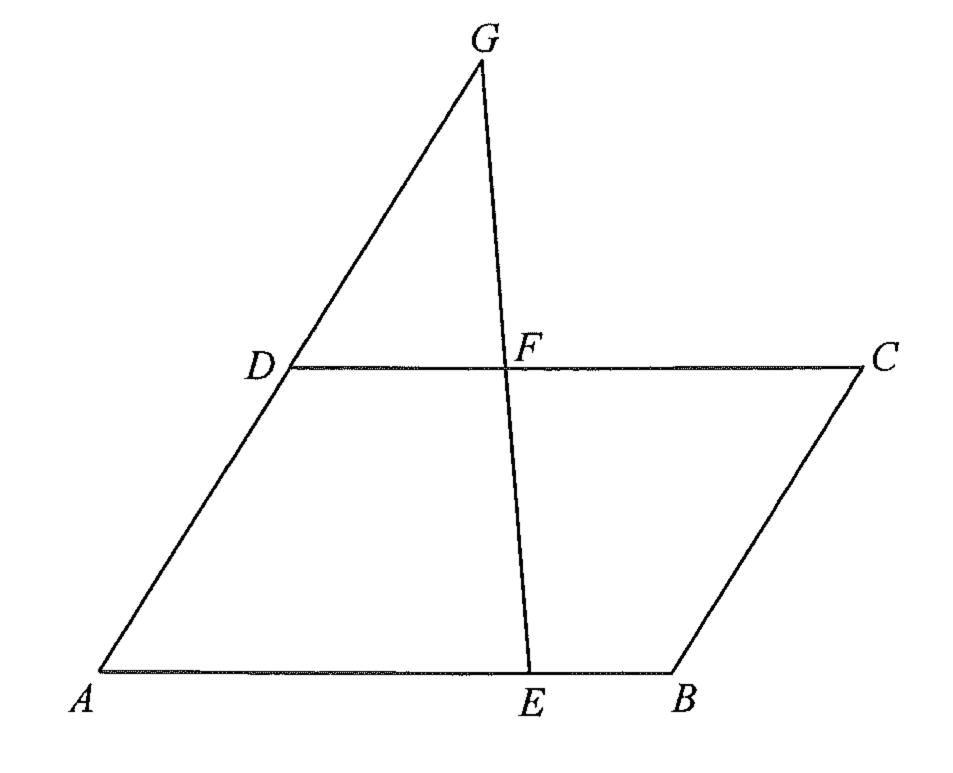


In the figure, ABCD is a parallelogram. E and F are points lying on AB and CD respectively. AD produced and EF produced meet at G. It is given that DF:FC=3:4 and AD:DG=1:1. If the area of  $\Delta DFG$  is  $3 \text{ cm}^2$ , then the area of the parallelogram ABCD is

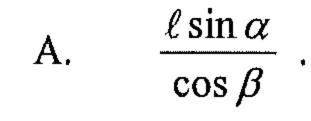
A. 
$$12 \text{ cm}^2$$
.

B. 
$$14 \text{ cm}^2$$
.

$$C. 18 cm^2.$$



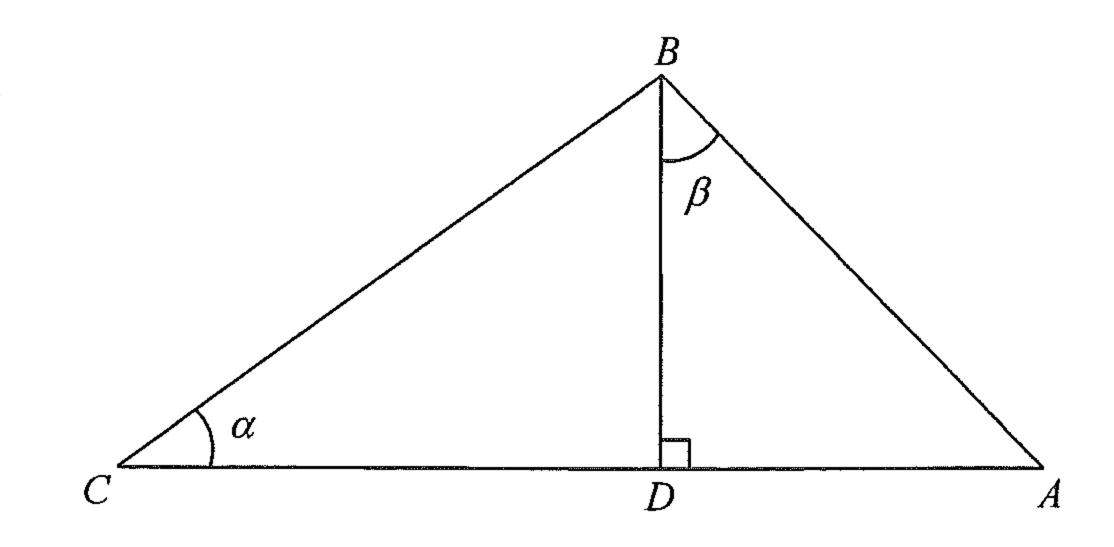
18. In the figure, D is a point lying on AC such that BD is perpendicular to AC. If  $BC = \ell$ , then  $AB = \ell$ 



B. 
$$\frac{\ell \sin \beta}{\cos \alpha}$$

C. 
$$\frac{\ell \cos \alpha}{\sin \beta}$$

D. 
$$\frac{\ell \cos \beta}{\sin \alpha}$$



19. 
$$\frac{\cos 60^{\circ}}{1 - \cos(90^{\circ} - \theta)} + \frac{\cos 240^{\circ}}{1 - \cos(270^{\circ} - \theta)} =$$

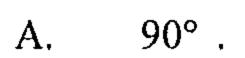
A. 
$$\frac{1}{\cos^2 \theta}$$
.

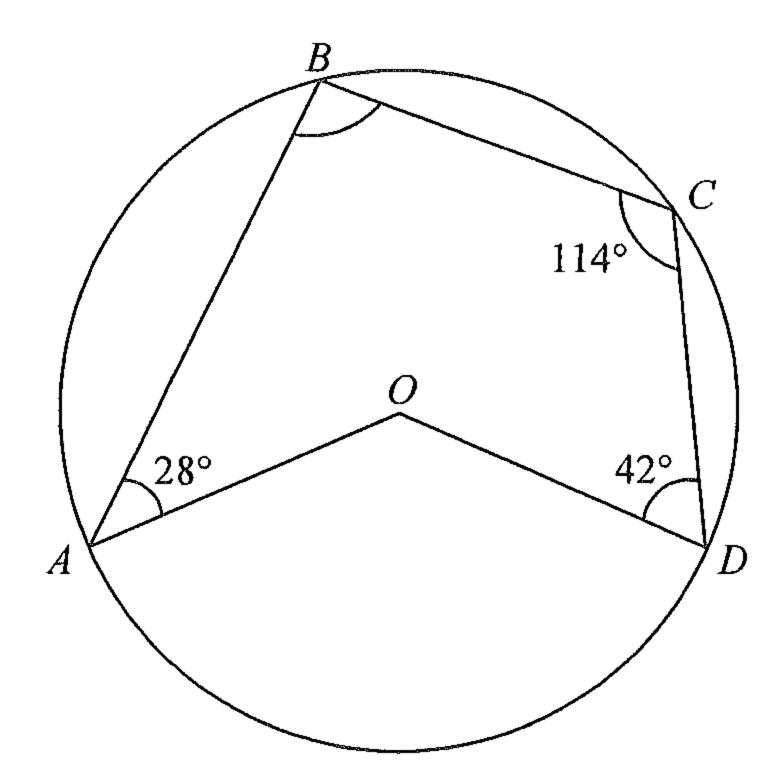
B. 
$$\frac{\cos\theta}{\tan\theta}$$
.

C. 
$$\frac{\tan \theta}{\cos \theta}.$$

D. 
$$\frac{1}{\cos\theta\tan\theta}$$

20. In the figure, O is the centre of the circle ABCD. If  $\angle BAO = 28^{\circ}$ ,  $\angle BCD = 114^{\circ}$  and  $\angle CDO = 42^{\circ}$ , then  $\angle ABC =$ 





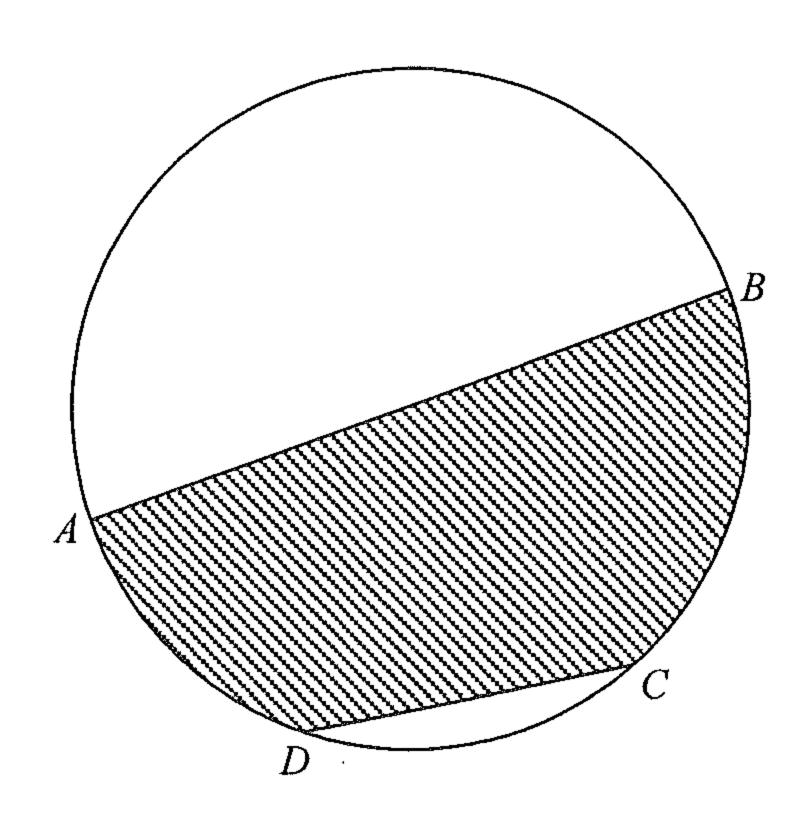
In the figure, AB is a diameter of the circle ABCD. If  $AB=12\,\mathrm{cm}$  and  $CD=6\,\mathrm{cm}$ , then the area of the shaded region is

A. 
$$(12\pi - 9) \text{ cm}^2$$
.

B. 
$$(12\pi + 9) \text{ cm}^2$$
.

C. 
$$(12\pi - 9\sqrt{3}) \text{ cm}^2$$
.

D. 
$$(12\pi + 9\sqrt{3}) \text{ cm}^2$$
.

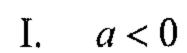


- 22. Which of the following statements about a regular 12-sided polygon are true?
  - I. Each exterior angle is 30°.
  - II. Each interior angle is 150°.
  - III. The number of axes of reflectional symmetry is 6.
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III

- 23. The rectangular coordinates of the point P are  $(-3, -3\sqrt{3})$ . If P is rotated anticlockwise about the origin through 90°, then the polar coordinates of its image are
  - A.  $(3,150^{\circ})$ .
  - B.  $(3,330^{\circ})$ .
  - C. (6,150°).
  - D.  $(6,330^{\circ})$ .

- 24. If P is a moving point in the rectangular coordinate plane such that the distance between P and the point (20,12) is equal to 5, then the locus of P is a
  - A. circle.
  - B. square.
  - C. parabola.
  - D. triangle.

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are ax + y = b and cx + y = d respectively. Which of the following are true?

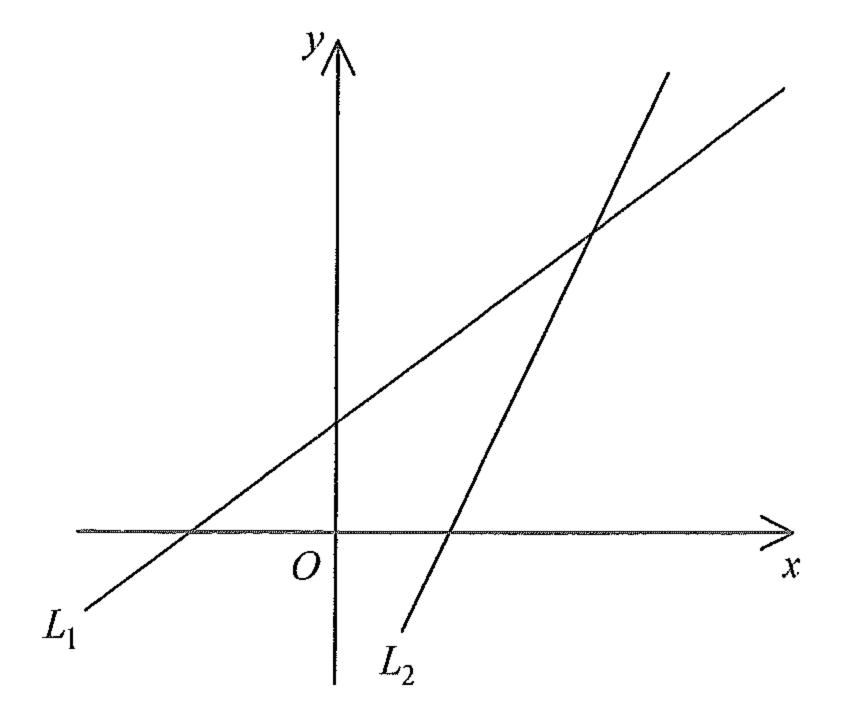


II. 
$$a < c$$

III. 
$$b > d$$

IV. 
$$ad > bc$$

- A. I, II and III only
- B. I, II and IV only
- C. I, III and IV only
- D. II, III and IV only

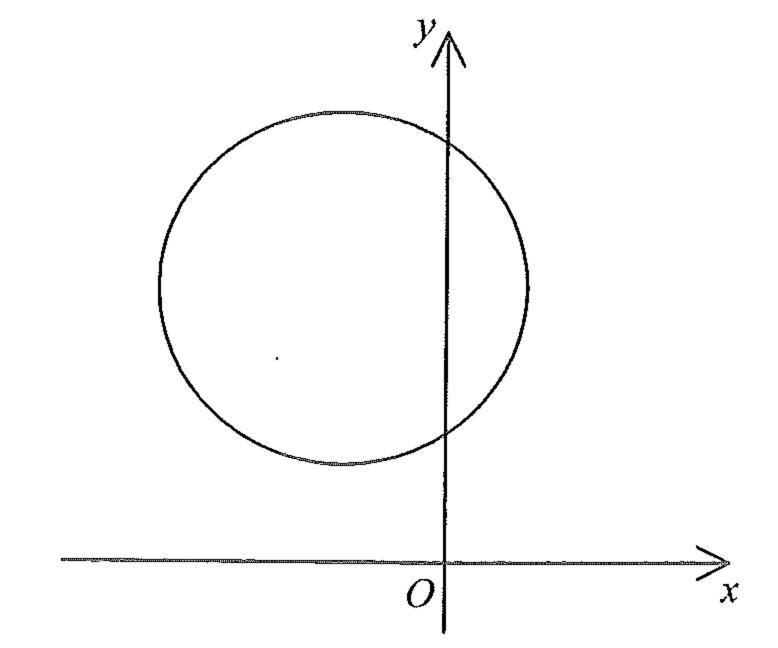


26. In the figure, the radius of the circle and the coordinates of the centre are r and (h, k) respectively. Which of the following are true?

I. 
$$h + k > 0$$

II. 
$$r-h>0$$

III. 
$$r-k>0$$



27. 9★♦ is a 3-digit number, where ★ and ♦ are integers from 0 to 9 inclusive. Find the probability that the 3-digit number is divisible by 5.

A. 
$$\frac{1}{2}$$

B. 
$$\frac{7}{33}$$

C. 
$$\frac{20}{99}$$

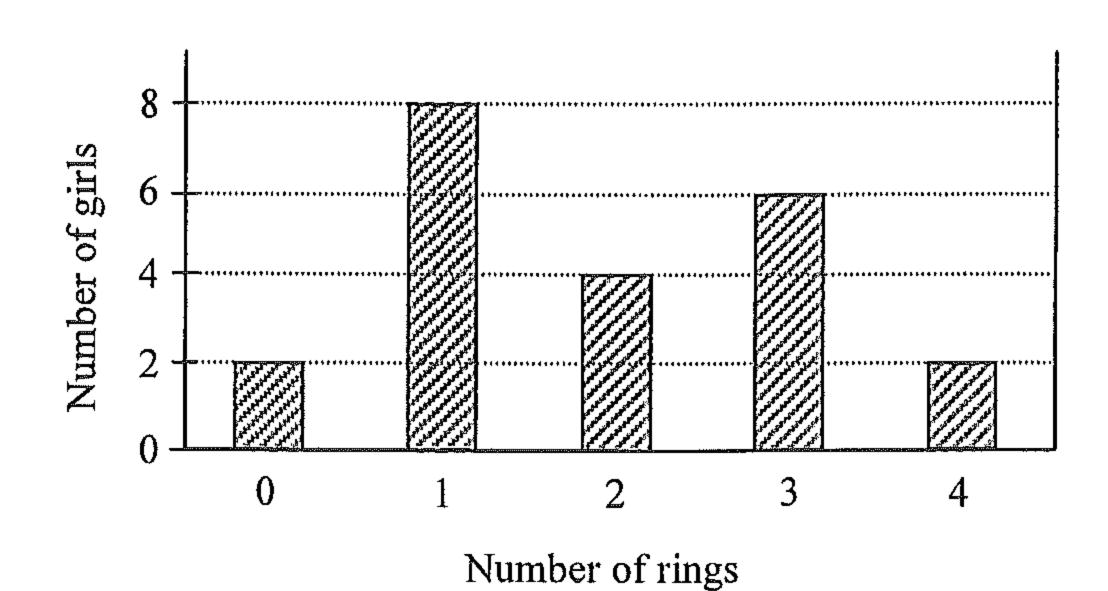
D. 
$$\frac{19}{100}$$

28. The stem-and-leaf diagram below shows the distribution of the ages of a group of members in a recreational centre.

Stem (tens)	Leaf (units)							
5	0	5	<del></del> 6	6	8			
6	1	4	5	5	7	8	8	9
7	3	4	4	6	7	9		
8								
9	1							

A member is randomly selected from the group. Find the probability that the selected member is not under the age of 74.

- A. 0.2
- B. 0.3
- C. 0.7
- D. 0.8
- 29. The bar chart below shows the distribution of the numbers of rings owned by the girls in a group. Find the standard deviation of the distribution correct to 2 decimal places.
  - A. 1.04
  - B. 1.16
  - C. 1.19
  - D. 2.09



30. Consider the following data:

- 19
- 10
- 12
- 12
- 13 13
- 14
- 15

16

n

If both the mean and the median of the above data are 14, which of the following are true?

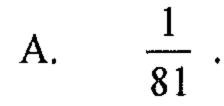
- I.  $\sqrt{m} \ge 14$
- II. *n* ≤ 16
- III. m + n = 30
  - A. I and II only
  - B. I and III only
  - C. II and III only
  - D. I, II and III

## **Section B**

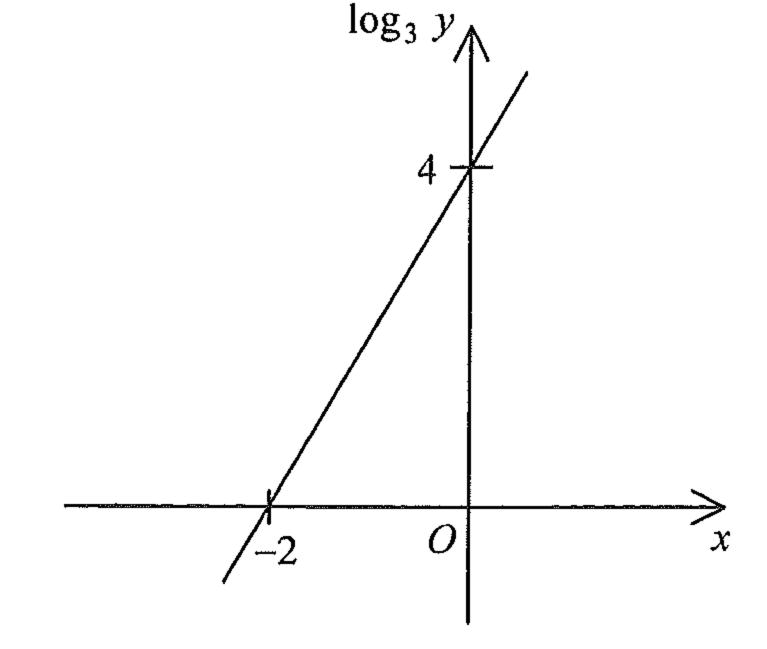
31. The H.C.F. and the L.C.M. of three expressions are  $ab^2$  and  $4a^4b^5c^6$  respectively. If the first expression and the second expression are  $2a^2b^4c$  and  $4a^4b^2c^6$  respectively, then the third expression is

- A.  $ab^2$ .
- B.  $ab^5$ .
- C.  $2ab^2c$ .
- D.  $2ab^5c$ .

32. The graph in the figure shows the linear relation between x and  $\log_3 y$ . If  $y = mn^x$ , then n =



- B.  $\frac{1}{9}$ .
- C. 9.
- D. 81.



33.  $AD0000002012_{16} =$ 

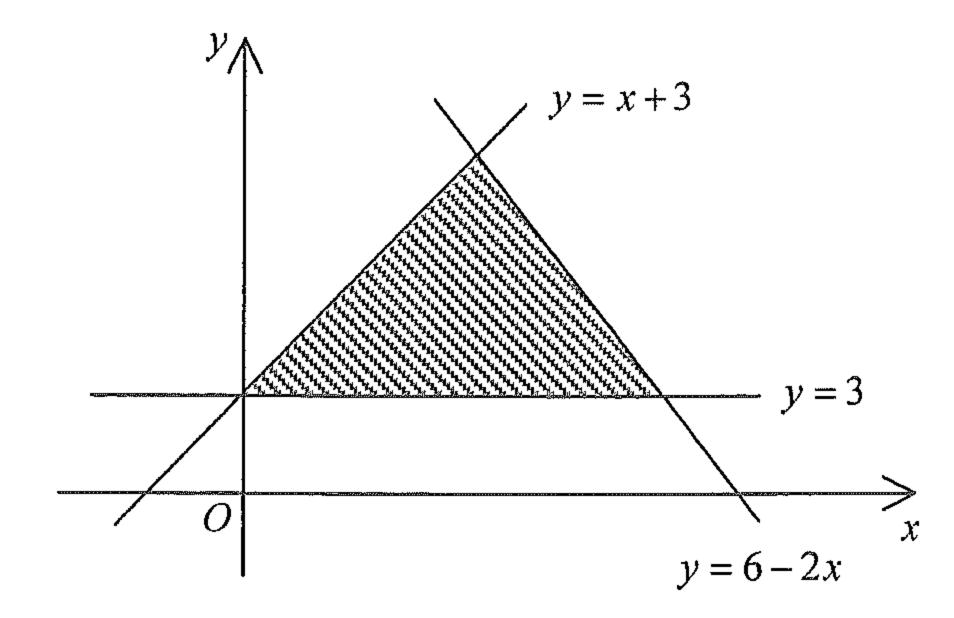
- A.  $(10)16^{11} + (13)16^{10} + 8210$ .
- B.  $(10)16^{12} + (13)16^{11} + 131360$ .
- C.  $(11)16^{11} + (14)16^{10} + 8210$ .
- D.  $(11)16^{12} + (14)16^{11} + 131360$ .

34. Let f(x) be a quadratic function. If the coordinates of the vertex of the graph of y = f(x) are (3, -4), which of the following must be true?

- A. The roots of the equation f(x) = 0 are integers.
- B. The roots of the equation f(x)-3=0 are rational numbers.
- C. The roots of the equation f(x)+4=0 are real numbers.
- D. The roots of the equation f(x) + 5 = 0 are nonreal numbers.

- 35.  $i^3(\beta i 3) =$ 
  - A.  $\beta + 3i$ .
  - B.  $\beta-3i$ .
  - C.  $-\beta + 3i$ .
  - D.  $-\beta 3i$ .

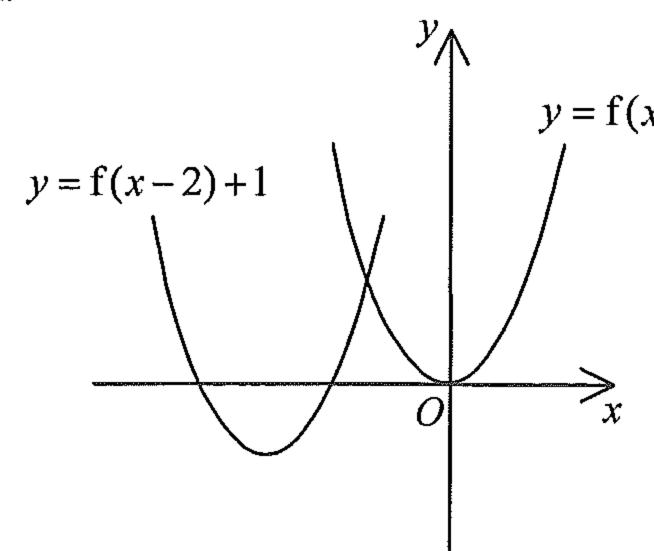
- 36. The figure shows a shaded region (including the boundary). If (h, k) is a point lying in the shaded region, which of the following are true?
  - I.  $k \ge 3$
  - II.  $h-k \ge -3$
  - III.  $2h+k \le 6$ 
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III



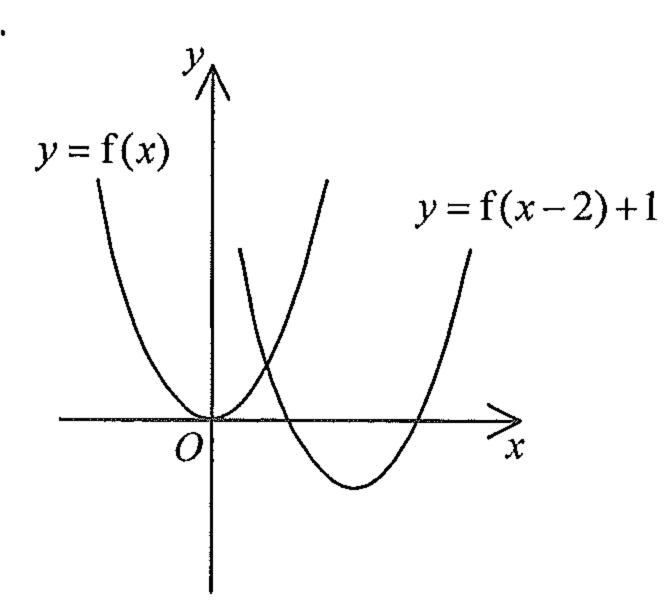
- 37. Let  $a_n$  be the *n*th term of an arithmetic sequence. If  $a_{18} = 26$  and  $a_{23} = 61$ , which of the following are true?
  - I.  $a_{14} < 0$
  - II.  $a_1 a_2 < 0$
  - III.  $a_1 + a_2 + a_3 + \dots + a_{27} > 0$ 
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III

Which of the following may represent the graph of y = f(x) and the graph of y = f(x-2)+1 on the same rectangular coordinate system?

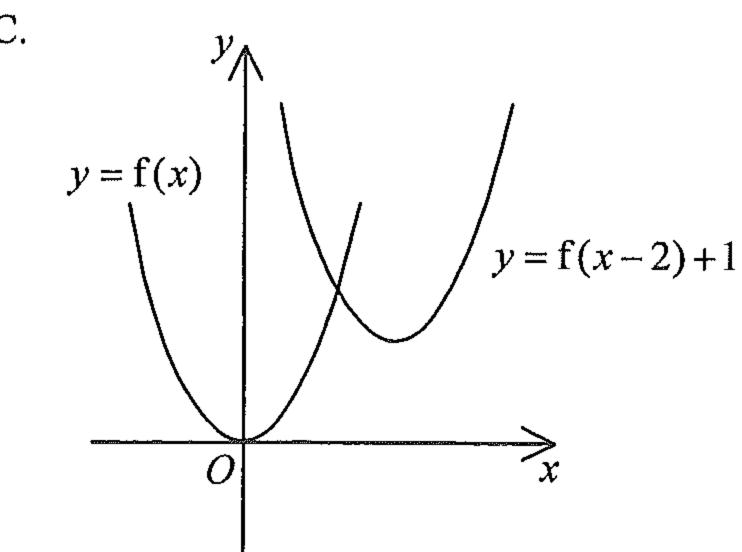
A.



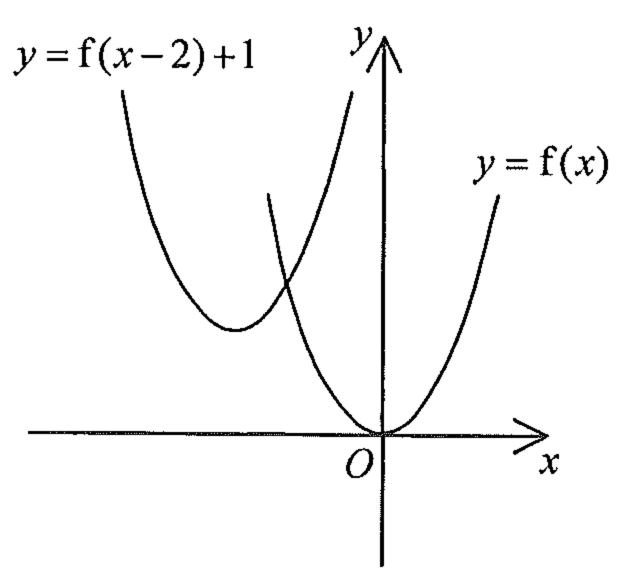
В



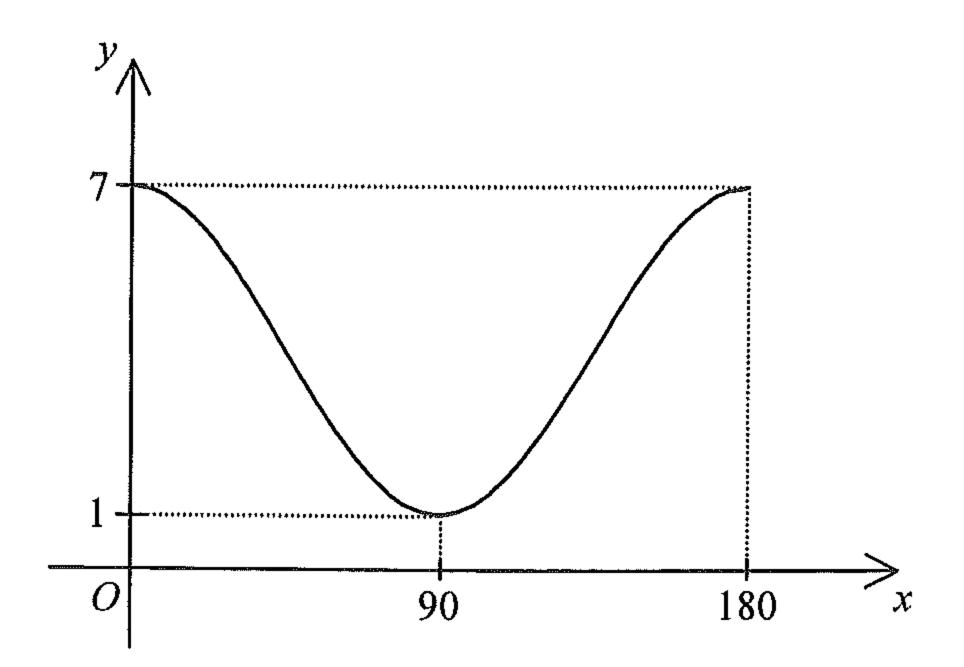
 $\mathbf{C}$ 



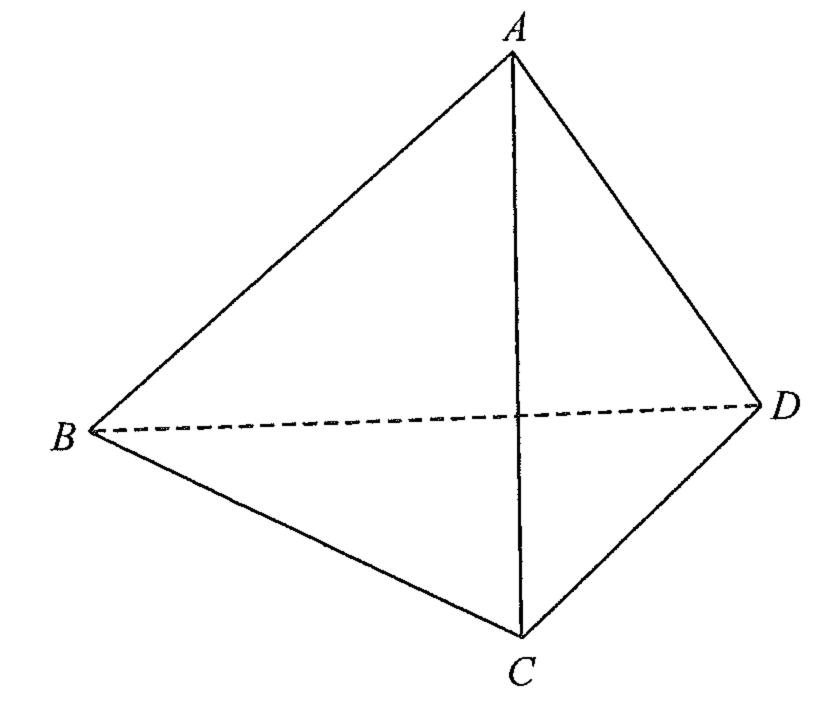
D.



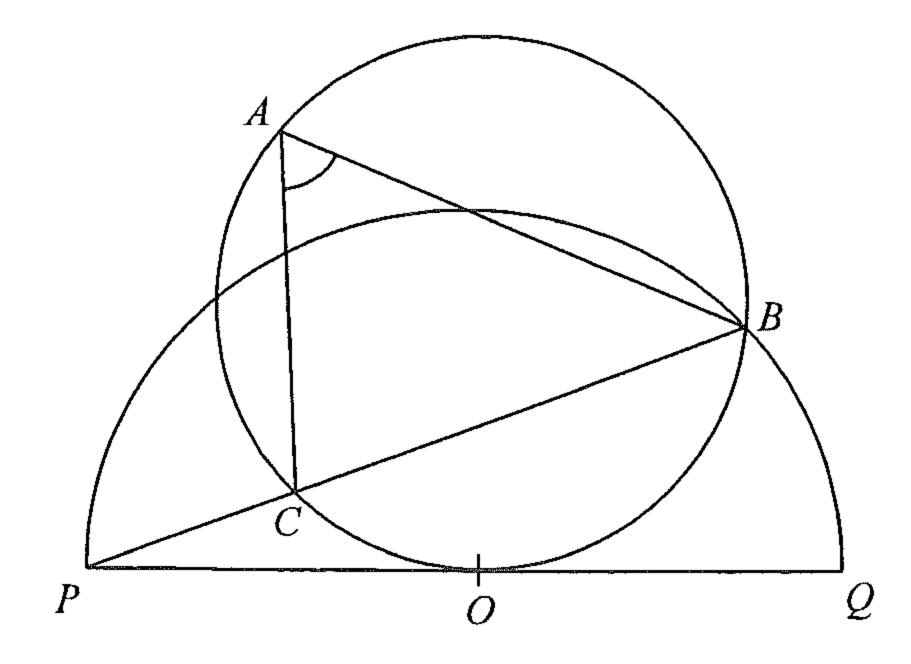
- 39. The figure shows
  - A. the graph of  $y = 1 + 3\cos\frac{x^{\circ}}{2}$ .
  - B. the graph of  $y = 1 + 3\cos 2x^{\circ}$ .
  - C. the graph of  $y = 4 + 3\cos\frac{x^{\circ}}{2}$ .
  - D. the graph of  $y = 4 + 3\cos 2x^{\circ}$ .



- 40. The figure shows a regular tetrahedron *ABCD*. Find the angle between the plane *ABC* and the plane *BCD* correct to the nearest degree.
  - A. 48°
  - B. 53°
  - C. 60°
  - D. 71°



- In the figure, PQ is the tangent to the circle ABC at O, where O is the centre of the semicircle PBQ. It is given that BCP is a straight line. If  $\angle BPQ = 12^{\circ}$ , then  $\angle BAC =$ 
  - A. 18°.
  - B. 24°.
  - C. 36°.
  - D. 54°.



- Find the range of values of k such that the circle  $x^2 + y^2 + 2x 4y 13 = 0$  and the straight line x y + k = 0 intersect at two distinct points.
  - A. -9 < k < 3
  - $^{\vee}$ B. -3 < k < 9
  - C. k < -9 or k > 3
  - D. k < -3 or k > 9

- 43. A drama club is formed by 12 boys and 8 girls. If a team of 5 students is selected from the club to participate in a competition and the team consists of at least one girl, how many different teams can be formed?
  - A. 3960
  - B. 14712
  - C. 15448
  - D. 15504
- 44. A box contains six balls numbered 7, 8, 8, 9, 9 and 9 respectively. John repeats drawing one ball at a time randomly from the box without replacement until the number drawn is 9. Find the probability that he needs exactly three draws.
  - A.  $\frac{1}{2}$
  - B.  $\frac{1}{6}$
  - C.  $\frac{1}{8}$
  - D.  $\frac{3}{20}$
- 45. Let  $m_1$ ,  $r_1$  and  $v_1$  be the mean, the range and the variance of a group of numbers  $\{x_1, x_2, x_3, \ldots, x_{100}\}$  respectively. If  $m_2$ ,  $r_2$  and  $v_2$  are the mean, the range and the variance of the group of numbers  $\{x_1, x_2, x_3, \ldots, x_{100}, m_1\}$  respectively, which of the following must be true?
  - I.  $m_1 = m_2$
  - II.  $r_1 = r_2$
  - III.  $v_1 = v_2$ 
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III

#### END OF PAPER