2014-DSE MATH CP PAPER 2

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2014

MATHEMATICS Compulsory Part PAPER 2

11.30 am - 12.45 pm (11/4 hours)

INSTRUCTIONS

- 1. Read carefully the instructions on the Answer Sheet. After the announcement of the start of the examination, you should first stick a barcode label and insert the information required in the spaces provided. No extra time will be given for sticking on the barcode label after the 'Time is up' announcement.
- 2. When told to open this book, you should check that all the questions are there. Look for the words 'END OF PAPER' after the last question.
- 3. All questions carry equal marks.
- 4. **ANSWER ALL QUESTIONS**. You are advised to use an HB pencil to mark all the answers on the Answer Sheet, so that wrong marks can be completely erased with a clean rubber. You must mark the answers clearly; otherwise you will lose marks if the answers cannot be captured.
- 5. You should mark only **ONE** answer for each question. If you mark more than one answer, you will receive **NO MARKS** for that question.
- 6. No marks will be deducted for wrong answers.

©香港考試及評核局 保留版權 Hong Kong Examinations and Assessment Authority All Rights Reserved 2014 Not to be taken away before the end of the examination session

There are 30 questions in Section A and 15 questions in Section B. The diagrams in this paper are not necessarily drawn to scale. Choose the best answer for each question.

Section A

1.
$$(2n^3)^{-5} =$$

A.
$$\frac{1}{32n^2}$$
.

B.
$$\frac{1}{32n^{15}}$$
.

C.
$$\frac{1}{10n^{125}}$$
.

D.
$$\frac{1}{10n^{243}}$$
.

2.
$$u^2 - v^2 - 5u + 5v =$$

A.
$$(u-v)(u+v-5)$$
.

B.
$$(u-v)(u+v+5)$$
.

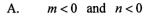
C.
$$(u+v)(u-v-5)$$
.

D.
$$(u+v)(u-v+5)$$
.

3. If p and q are constants such that
$$px(x-1) + x^2 = qx(x-2) + 4x$$
, then $p =$

- A. 1.
- B. 2.
- C. 3.
- D. 4.

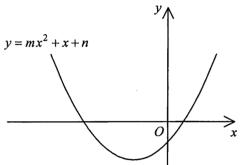
- 4. Let a be a constant. If the quadratic equation $x^2 + ax + a = 1$ has equal roots, then a =
 - A. -1.
 - B. 2.
 - C. 0 or -4.
 - D. 0 or 4.
- 5. The figure shows the graph of $y = mx^2 + x + n$, where m and n are constants. Which of the following is true?



B.
$$m < 0$$
 and $n > 0$

C.
$$m > 0$$
 and $n < 0$

D.
$$m > 0$$
 and $n > 0$



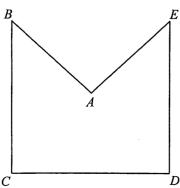
- 6. If a > b and k < 0, which of the following must be true?
 - I. $a^2 > b^2$
 - II. a+k>b+k

III.
$$\frac{a}{k^2} > \frac{b}{k^2}$$

- A. I only
- B. II only
- C. I and III only
- D. II and III only
- 7. The solution of -3x < 6 < 2x is
 - A. x > -2.
 - B. x > 0.
 - C. x > 3.
 - D. -2 < x < 3.

- 8. The price of 2 bowls and 3 cups is \$506. If the price of 5 bowls and the price of 4 cups are the same, then the price of a bowl is
 - A. \$88.
 - B. \$92.
 - C. \$110.
 - D. \$115.
- 9. There are 792 workers in a factory. If the number of male workers is 20% less than that of female workers, then the number of male workers is
 - A. 352.
 - B. 360.
 - C. 432.
 - D. 440.
- 10. If the angle and the radius of a sector are decreased by x% and 50% respectively so that its area is decreased by 90%, then x =
 - A. 20.
 - B. 40.
 - C. 60.
 - D. 80.
- 11. The width and the length of a thin rectangular metal sheet are measured as 8 cm and 10 cm correct to the nearest cm respectively. Let $x \text{ cm}^2$ be the actual area of the metal sheet. Find the range of values of x.
 - A. $71.25 \le x < 89.25$
 - B. $71.25 < x \le 89.25$
 - C. $79.5 \le x < 80.5$
 - D. $79.5 < x \le 80.5$

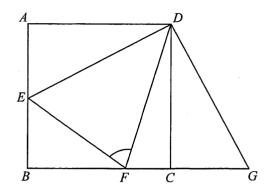
- 12. It is given that $\frac{4}{5a} = \frac{5}{7b} = \frac{7}{9c}$, where a, b and c are positive numbers. Which of the following is true?
 - A. a < b < c
 - B. a < c < b
 - C. b < a < c
 - D. b < c < a
- 13. If z varies inversely as x and directly as the cube of y, which of the following must be constant?
 - A. xy^3z
 - B. x^3yz^3
 - C. $\frac{y^3}{xz}$
 - D. $\frac{y}{x^3z^3}$
- 14.. Let a_n be the *n*th term of a sequence. If $a_2 = 7$, $a_4 = 63$ and $a_{n+2} = a_{n+1} + a_n$ for any positive integer n, then $a_5 =$
 - A. 56.
 - B. 70.
 - C. 91.
 - D. 119.
- 15. In the figure, AB = AE and $\angle BAE = \angle BCD = \angle CDE = 90^{\circ}$. If BC = CD = DE = 16 cm, then the area of the pentagon ABCDE is
 - A. $71 \,\mathrm{cm}^2$.
 - B. 128 cm^2 .
 - C. 192 cm^2 .
 - D. 224 cm^2 .



16. In the figure, ABCD is a square. BC is produced to G such that $\angle CDG = 25^{\circ}$. E is a point lying on AB such that AE = CG. If F is a point lying on BC such that $\angle CDF = 20^{\circ}$, then $\angle DFE = 10^{\circ}$







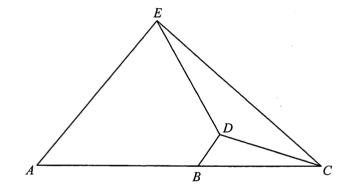
17. In the figure, B is a point lying on AC such that AB:BC=3:2. It is given that $AE/\!\!/BD$. If the area of ΔBCD and the area of ΔCDE are 4 cm^2 and 8 cm^2 respectively, then the area of the trapezium ABDE is

A.
$$18 \,\mathrm{cm}^2$$
.

B.
$$21 \,\mathrm{cm}^2$$
.

C.
$$27 \text{ cm}^2$$
.

D.
$$33 \,\mathrm{cm}^2$$
.



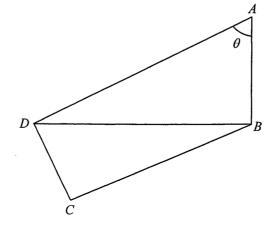
18. In the figure, $\angle ABD = \angle ADC = \angle BCD = 90^{\circ}$. If $AB = \ell$, then $CD = 20^{\circ}$



B.
$$\ell \cos \theta$$
.

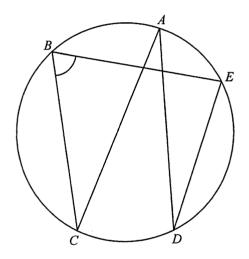
C.
$$\ell \sin \theta \tan \theta$$
.

D.
$$\frac{\ell \tan \theta}{\cos \theta}$$

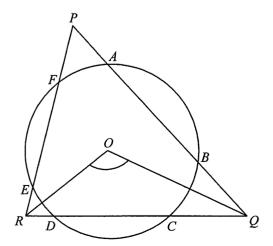


- 19. $(\cos(90^{\circ} + \theta) + 1)(\sin(360^{\circ} \theta) 1) =$
 - A. $-\cos^2\theta$.
 - B. $-\sin^2\theta$.
 - C. $\cos^2 \theta$.
 - D. $\sin^2 \theta$.

- 20. In the figure, AC is a diameter of the circle ABCDE. If $\angle ADE = 28^{\circ}$, then $\angle CBE =$
 - A. 56°.
 - B. 62°.
 - C. 72°.
 - D. 76°.



- 21. In the figure, O is the centre of the circle ABCDEF. $\triangle PQR$ intersects the circle at A, B, C, D, E and F. If $\angle QPR = 38^{\circ}$ and AB = CD = EF, then $\angle QOR =$
 - A. 109°.
 - B. 117°.
 - C. 123°.
 - D. 142°.



If an interior angle of a regular n-sided polygon is greater than an exterior angle by 100°, which of the following are true?
I. The value of n is 10.
II. Each exterior angle of the polygon is 40°.

III. The number of axes of reflectional symmetry of the polygon is 9.

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III
- 23. The rectangular coordinates of the point P are $(-1, \sqrt{3})$. If P is reflected with respect to the x-axis, then the polar coordinates of its image are
 - A. (2,210°).
 - B. (2,240°).
 - C. $(4,210^{\circ})$.
 - D. (4, 240°).

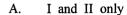
- 24. The equations of the straight lines L_1 and L_2 are 2x+3y=5 and 4x+6y=7 respectively. If P is a moving point in the rectangular coordinate plane such that the perpendicular distance from P to L_1 is equal to the perpendicular distance from P to L_2 , then the locus of P is a
 - A. circle.
 - B. square.
 - C. parabola.
 - D. straight line.

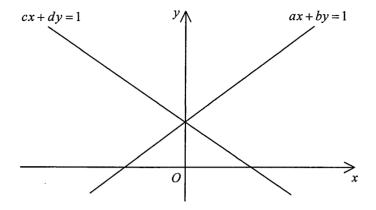
25. In the figure, the two straight lines intersect at a point on the positive y-axis. Which of the following are true?



II.
$$c > 0$$

III.
$$b = d$$

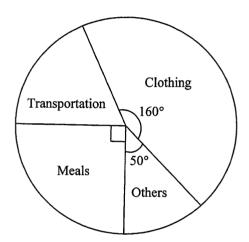




26. If a diameter of the circle $x^2 + y^2 - 8x + ky - 214 = 0$ passes through the point (6, -5) and the slope of the diameter is -4, then k =

27. A box contains m yellow balls and 20 black balls. If a ball is randomly drawn from the box, then the probability of drawing a yellow ball is $\frac{1}{m}$. Find the value of m.

- 28. The mean height of 25 teachers and 140 students is 150 cm. If the mean height of the students is 145 cm, then the mean height of the teachers is
 - A. 151 cm.
 - B. 155 cm.
 - C. 176 cm.
 - D. 178 cm.
- 29. The pie chart below shows the expenditure of John in a certain week. John spends \$240 on clothing that week. Find his expenditure on transportation that week.
 - A. \$40
 - B. \$60
 - C. \$90
 - D. \$135



30. The stem-and-leaf diagram below shows the distribution of the ages of the passengers in a bus.

| Stem (tens) | Lea | ıf (uni | ts) | | | | |
|-------------|-----|------------------|-----|---|---|---|---|
| 1 | h | 4 | 6 | | | | |
| 2 | 3 | 3 | 3 | 4 | 6 | 7 | 7 |
| 3 | 1 | 2 | 2 | 2 | 6 | 8 | |
| 4 | 0 | \boldsymbol{k} | | | | | |

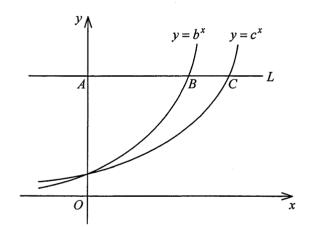
If the range of the above distribution is at least 33, which of the following must be true?

- I. $0 \le h \le 3$
- II. $3 \le k \le 9$
- III. $3 \le k h \le 5$
 - A. I only
 - B. II only
 - C. I and III only
 - D. II and III only

Section B

- 31. The H.C.F. of $3x^4y^2z$, $4xy^5z$ and $6x^2y^3$ is
 - A. xy^2
 - B. xy^2z .
 - C. $12x^4y^5z$.
 - D. $12x^7y^9z^2$.

- 32. The figure shows the graph of $y = b^x$ and the graph of $y = c^x$ on the same rectangular coordinate system, where b and c are positive constants. If a horizontal line L cuts the y-axis, the graph of $y = b^x$ and the graph of $y = c^x$ at A, B and C respectively, which of the following are true?
 - I. b < c
 - II. bc > 1
 - III. $\frac{AB}{AC} = \log_b c$
 - A. I and II only
 - B. I and III only
 - C. II and III only
 - D. I, II and III

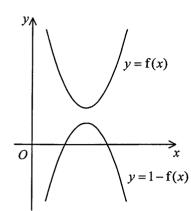


- 33. Which of the following is the greatest?
 - A. 124²⁴¹
 - B. 241²¹⁴
 - C. 412¹⁴²
 - D. 421¹²⁴

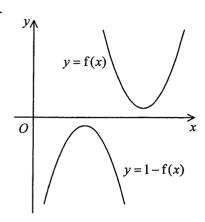
- 34. $7 \times 2^{10} + 2^8 + 5 \times 2^3 2^3 =$
 - A. 111010100000₂.
 - B. 111100010000₂.
 - C. 1110100100000₂.
 - D. 1111000010000₂.
- 35. Let $f(x) = 3x^2 6x + k$, where k is a constant. If the y-coordinate of the vertex of the graph of y = f(x) is 7, then $k = x^2 6x + k$
 - A. 1.
 - B. 3.
 - C. 4.
 - D. 10.
- 36. If β is a real number, then $\frac{\beta^2 + 4}{\beta + 2i} =$
 - A. $\beta 2i$.
 - B. $\beta + 2i$.
 - C. $2-\beta i$.
 - D. $2 + \beta i$.
- 37. If m > 1, which of the following are geometric sequences?
 - I. 2^m , 2^{2m} , 2^{3m} , 2^{4m}
 - II. m, $2m^2$, $3m^4$, $4m^8$
 - III. $\log m$, $\log m^2$, $\log m^4$, $\log m^8$
 - A. I and II only
 - B. I and III only
 - C. II and III only
 - D. I, II and III

38. Which of the following may represent the graph of y = f(x) and the graph of y = 1 - f(x) on the same rectangular coordinate system?

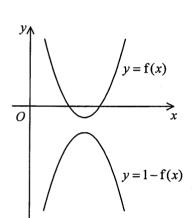
A.



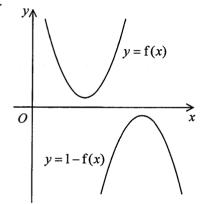
B.



C.



D.



- 39. For $0^{\circ} \le x \le 360^{\circ}$, how many roots does the equation $7 \sin^2 x = \sin x$ have?
 - A. 2
 - B. 3
 - C. 4
 - D. 5

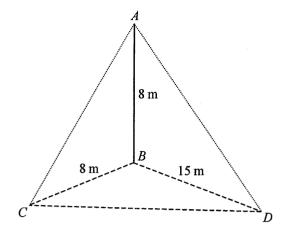
40. In the figure, AB is a vertical pole standing on the horizontal ground BCD, where $\angle CBD = 90^{\circ}$. If the angle between the plane ACD and the horizontal ground is θ , then $\tan \theta =$





C. $\frac{15}{17}$.

D. $\frac{17}{15}$.



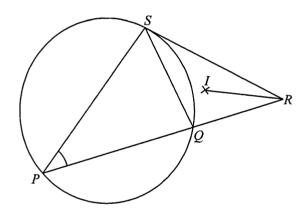
41. In the figure, PQS is a circle. PQ is produced to R such that RS is the tangent to the circle at S. I is the in-centre of $\triangle QRS$. If $\angle IRQ = 12^{\circ}$ and $\angle PSQ = 70^{\circ}$, then $\angle QPS =$

A. 24°.

B. 37°.

C. 43°.

D. 62°.



42. If the straight line x-y=k and the circle $x^2+y^2+2x-4y-1=0$ intersect at A and B, then the x-coordinate of the mid-point of AB is

A. 1+k.

B. 1-k.

 $C. \qquad \frac{1+k}{2} \ .$

 $D. \qquad \frac{1-k}{2} \ .$

| 43. | There are 13 boys and 17 girls in a class. If a team of 2 boys and 3 girls is selected from the class to participate in a voluntary service, how many different teams can be formed? | | | | | | | |
|-----|--|---|---|--|--|--|--|--|
| | | A. | 38 896 | | | | | |
| | | B. | 53 040 | | | | | |
| | | C. | 142 506 | | | | | |
| | | D. | 636 480 | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| 44. | | In an examination, Peter gets 55 marks and his standard score is -3 while Mary gets 95 marks and standard score is 2 . Find the mean of the examination scores. | | | | | | |
| | | A. | 8 marks | | | | | |
| | | B. | 64 marks | | | | | |
| | | C. | 75 marks | | | | | |
| , | | D. | 79 marks | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| 45. | If the $14-b$ | variance , 14 – | of the four numbers a , b , c and d is 9 , then the variance of the four numbers $14-a$, c and $14-d$ is | | | | | |
| | | A. | 5. | | | | | |
| | | B. | 9. | | | | | |
| | | C. | 23. | | | | | |
| | | D. | 121. | | | | | |
| | | | | | | | | |
| | | | | | | | | |