

PAPER 1

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2021

MATHEMATICS Compulsory Part PAPER 1

Question-Answer Book

 $8:30 \text{ am} - 10:45 \text{ am} (2\frac{1}{4} \text{ hours})$ This paper must be answered in English

INSTRUCTIONS

- (1) After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- (2) This paper consists of THREE sections, A(1), A(2) and B.
- (3) Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- (4) Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- (5) Unless otherwise specified, all working must be clearly shown.
- (6) Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
- (7) The diagrams in this paper are not necessarily drawn to scale.
- (8) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

@香港考試及評核局 保留版權 Hong Kong Examinations and Assessment Authority All Rights Reserved 2021

Please stick the barcode label here.
Candidate Number



ked.	
mar	
ot be	
will no	
nargins	
the r	
Ξ.	
written	
Answers written in the margins will not be marked.	

3.	Factor	rize
		$6x^2 + xy - 2y^2 ,$
	(b)	$8x - 4y - 6x^2 - xy + 2y^2 (3 marks)$
		(3 marks)
4.	(a)	Find the range of values of x which satisfy both $\frac{7(x-2)}{5} + 11 > 3(x-1)$ and $x+4 \ge 0$.
	(b)	How many positive integers satisfy both inequalities in (a)? (4 marks)
	*	

stickers to the	of stickers owned girl, then the n number of sticke	umber of sticker	rs owned by the boy and the girl.	girl is 2 time	es that owned	d by the (4 ma
***************************************			//////////////////////////////////////			
			ost by \$80 . Th			
			ost by \$80 . The ercentage profit			d price of
its marked pri						d price of
its marked pri						
its marked pri						d price of
its marked pri						d price of
its marked pri						d price of
its marked pri						d price of

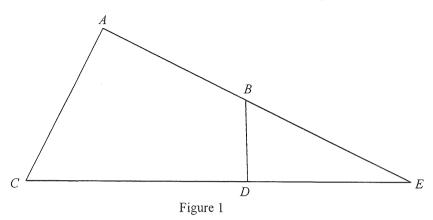
Please stick the barcode label here.

are	polar coordinate system, O is the pole. The polar coordinates of the points P and $Q(r, 80^\circ)$ and $Q(r, 140^\circ)$ respectively, where P is a positive constant. It is given that the distance P and Q is 21. Find
(a)	$\angle POQ$,
(b)	r ,
(c)	the perimeter of ΔOPQ .
	(4 marks

,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	

(5 marks)

8. In Figure 1, AB produced and CD produced meet at the point E. It is given that $\angle CAE = \angle BDE$.

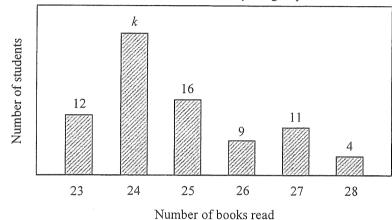


- (a) Prove that $\triangle ACE \sim \triangle DBE$.
- (b) It is given that AC = 25 cm, AE = 60 cm, CE = 65 cm and BD = 15 cm.
 - (i) Is $\triangle ACE$ a right-angled triangle? Explain your answer.
 - (ii) Find the area of $\triangle BDE$.

,		
		1,

9. The bar chart below shows the distribution of the numbers of books read by a group of students in a year.

Distribution of the numbers of books read by the group of students in the year



If a student is randomly selected from the group, then the probability that the selected student reads fewer than 26 books in the year is $\frac{7}{10}$.

- (a) Find k.
- (b) Write down the range, the inter-quartile range and the standard deviation of the distribution. (5 marks)

Answers written in the margins will not be marked.

~i
ನ
Ž
Ξ
ā
Ξ
۸۵
č
5
ž
_
=
>
_
\mathbf{S}
Ħ
ы
Ξ
2
=
Φ
٩
+-
П
Answers written in the margins will not be marked.
ä
೭
=
Н
≥
ro
1
é
⋈
\sim
5
⋖

SEC	TION	A(2) (35 marks)	
0.		given that $f(x)$ is partly constant and partly varies as $(x+4)^2$. Suppose that $f(2) = 105$.	f(-3)=0
	(a)	Find $f(0)$.	(3 marks)
	(b)	Denote the graph of $y = f(x) + 3$ by G .	
		(i) Write down the y -intercept of G .	
		(ii) Find the x-intercept(s) of G .	(3 marks)
	10711741777111W		

			aalaa irgaatu

	41111111111		

Please stick the	barcode :	label	here
------------------	-----------	-------	------

 (b) Are the median and the mode of the distribution equal? Explain your answer. (c) If n more children play the game and each of them gets 5 tokens, write down (i) the value of n such that the mean of the distribution is increased by 1; (ii) the least value of n such that the median of the distribution is increased by 2; (iii) the greatest value of n such that the mode of the distribution remains unchanged. 	(a) Find the mean of the distribution.(b) Are the median and the mode of the distribution equal? Explain your answer.	1
 (b) Are the median and the mode of the distribution equal? Explain your answer. (c) If n more children play the game and each of them gets 5 tokens, write down (i) the value of n such that the mean of the distribution is increased by 1; (ii) the least value of n such that the median of the distribution is increased by 2; (iii) the greatest value of n such that the mode of the distribution remains unchanged. 	(b) Are the median and the mode of the distribution equal? Explain your answer.	
 (c) If n more children play the game and each of them gets 5 tokens, write down (i) the value of n such that the mean of the distribution is increased by 1; (ii) the least value of n such that the median of the distribution is increased by 2; (iii) the greatest value of n such that the mode of the distribution remains unchanged. 		(2 r
 (i) the value of n such that the mean of the distribution is increased by 1; (ii) the least value of n such that the median of the distribution is increased by 2; (iii) the greatest value of n such that the mode of the distribution remains unchanged. 	(c) If n more children play the game and each of them gets 5 tokens, write down	(2 r
(ii) the least value of n such that the median of the distribution is increased by 2; (iii) the greatest value of n such that the mode of the distribution remains unchanged.		
(iii) the greatest value of n such that the mode of the distribution remains unchanged.	(i) the value of n such that the mean of the distribution is increased by 1;	
	(ii) the least value of n such that the median of the distribution is increased by 2	;
	(iii) the greatest value of n such that the mode of the distribution remains unchanged	ged. (3 r
		,
)
		.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
		PW144-41-41-41-41-41-41-41-41-41-41-41-41-

(a)	Find c .			(3 mark
(b)	Prove that $x+3$ is a factor of $p(x)$.			(1 mar
(c)	Someone claims that all the roots of the equation correct? Explain your answer.	p(x) = 0	are real numbers.	Is the cla
				,
.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				

		naaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa		
.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				

Please stick the barcode label here.

	-
	7
	Los Junean Cal + Car Ilian Series Ser
	11:11:
	-

(a)	Find OG .	(2 marks
(b)	Does O lie inside C? Explain your answer.	(1 marl
(c)	Let P be a moving point in the rectangular coordinate plane such that OP = the locus of P by Γ . Suppose that Γ cuts C at the points M and N . F the quadrilateral $OMGN$.	GP . Deno ind the area (4 mark

ģ.
marke
I not be
in the margins will not be marked.
he marg
an in t

The l	the context T and equal. The transfer of the solid right circular cone Z is equal to the sum of the volume of X and case radius of Z is equal to the base diameter of X . A craftsman finds that	it the volume of
is 80	$00\pi~\mathrm{cm}^3$.	
(a)	Find the base radius of Y .	(2 mark
(b)	Are Y and Z similar? Explain your answer.	(3 marl
(c)	The craftsman claims that the sum of the curved surface area of X and the of Y is greater than the curved surface area of Z . Do you agree? Explain you	curved surface as our answer. (3 mar)

Harrison		

(4.,		
.,(
nambana a		

				40		

					-	
ked.				***************************************		ked.
maı		National Control of Co			·	 maı
ot be						ot be
/ill n						/ill n
ins w						 ins w
narg						 Answers written in the margins will not be marked.
the n						the r
Answers written in the margins will not be marked.						n in
vritte						vritte
ers v			74			ers v
vnsw						 \nsw
4						

		-				
	l					- [

	ONI	3 (35 marks)	
5	A que	eue is randomly formed by 7 teachers and 3 students.	
((a)	How many different queues can be formed?	(1 mark
((b)	Find the probability that no students are next to each other in the queue.	(3 marks

•••			

***	***************************************		

***	***************************************		
144			·
urs	*******************************		

,	marked.
	þe
	not
	_
	M
	Shroins
	a
	4
l	2.
	servers written in the margins will not be
	1
1	1
	č
1	2

Let .	A(n) be the <i>n</i> th term of an arithmetic sequence. It is given that $A(5) = 26$ and $A(12)$	-01.
(a)	Find $A(1)$.	(2 marks)
(b)	Suppose that $\log_2 G(n) = A(n)$ for any positive integer n . Find the greatest value of k such that $\log_8 (G(1)G(2)G(3)\cdots G(k)) < 999$.	(5 marks
Specialistic		
-eparatrolarith		
,,,,,,,,,,,,,,,,		-
· ·		

						
	ł					
]					
	1					
- 1						

- 1						
- 1						
- 1	,					
ı						
- 1						
- 1						
- 1					***************************************	
- 1						
ı						
- 1						
- 1					······································	
-						
- 1						
- 1						
- 1						
- 1						
-						
J						
- 1						
.						
۱۶						
will fill of illarned						
⊒ I						
31						
7						
۱ ⊱						
٦ ا						
5						
≓			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
≓						
ا ج						
31						
emg						
ا≃						
WITHER III HIE HA				***************************************		
7						
۱ ⊱						
3			***************************************	***************************************		v/**********
=						
<u> </u>						
51						
ا ت						
31						
۶						
اه						
3					***************************************	
۱ ٤						
C IO W CITY						
21		***************************************				
٦						
1						
- 1						
- [
- 1						
- 1						
- 1		***************************************				
- 1						
- 1						
- 1						
- [
- 1						
-1						
-						
- 1						
				.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		***************************************
ĺ						
-						
- 1						***************************************
- 1						
١						
- 1						,
- [***************************************			
- [
- 1						***************************************
- 1						

- A thin metal sheet ABCD is in the shape of a trapezium, where $AD/\!/BC$. It is given 18. (a) that AB = 45 cm, $\angle ADC = 70^{\circ}$ and $\angle BAD = 50^{\circ}$. Find CD. (2 marks)
 - The metal sheet ABCD described in (a) is now given. Let E be a point lying on AD such that (b) BE is perpendicular to AD. The metal sheet is folded along BE such that AE is perpendicular to the plane BCDE. Three thin triangular metal sheets are placed to this folded metal sheet to form a pyramid (see Figure 2). It is found that BC = 40 cm.

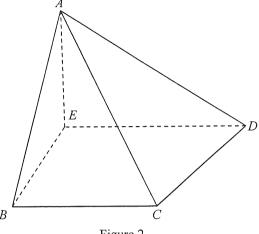


Figure 2

- Find $\angle CAD$. (i)
- Does the angle between the plane ACD and the plane BCDE exceed 30°? Explain (ii) your answer. (5 marks)

wannanna	 				 				.11011111111111111111111111111111111111

***************************************			***************************************		 ***************************************				,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

-110/1000	 				 				
***************************************	 			***************************************	 		***************************************		

***************************************	 			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	 .,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	***************************************			
***************************************	 		***************************************		 				***********

***************************************	 		······································		 				

***************************************	 				 		<i></i>		
100000000000000000000000000000000000000	 			***************************************	 				
	 				 				,,
	 	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,			 			dandari, markini da	
***************************************	 ·····			······································	 				
,	 				 			.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	

	 				 				,,,,,,,,,,,,

d.	١
ര്	۱
Ž.	1
=	١
ಡ	l
${f z}$	ŀ
	ļ
Ō	ı
\Box	I
ب	۱
Q.	Ì
⊏	I
_	l
=	
≥	ı
_	١
S	ı
\Box	ı
Ε,	ļ
£	١
ਕ	١
č	١
\Box	ı
Ch.	1
ā	ı
₽	
$\overline{}$	1
=	ı
Answers written in the margins will not be marked.	ı
<u>a</u>	Į
ř.	į
Ξ	
Ξ	1
≍	
· ^	i
Ľ	1
O	
≳	
50	
ď	
コ	
4	

).	coord	linate $f(14)$	$x^2-12kx-14x+36k^2+89k+53$, where k is a positive constant. On the satisfactor, denote the vertex of the graph of $y=f(x)$ and the vertex $(x-x)$ by $(x-x)$ by $(x-x)$ and $(x-x)$ by $(x-x$	of the graph
	(a)	Using	g the method of completing the square, express, in terms of k , the coordinate	s of Q . (2 marks)
	(b)	Write	e down, in terms of k , the coordinates of R .	(1 mark)
	(c)	The	coordinates of the point S are $(7, 4-3k)$. Denote the inscribed circle of Δ	QRS by C .
		(i)	Express, in terms of k , the equation of the straight line which passes through	gh Q and S .
		(ii)	Express, in terms of k , the equation of C .	
		(iii)	Suppose that QS is the tangent to C at the point T . Let U be the cent given that the coordinates of the point V are $(-29, -14)$. Is it possible to rectangle? Explain your answer.	tre of C . It is hat $STUV$ is a
			rectangle: Explain your answer.	(9 marks)

		,		
	A11147PHP1(199			
	***************************************	.4		
	.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,			

	 ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				
	 		17-111-111-11-11-11-11-11-11-11-11-11-11		
<i></i>					
	 			.,	 ***************************************
***************************************	 	dolarina			

	 			***************************************	 ***************************************

					v.
	,				

	 ,	,			
		***************************************			 ······································

			•		
(1/4-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-	 			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,					
	 ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		······································	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
	 		pr.)		

END OF PAPER	