2020-DSE MATH EP M1

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2020

## MATHEMATICS Extended Part Module 1 (Calculus and Statistics) Question-Answer Book

8:30 am – 11:00 am (2½ hours)
This paper must be answered in English

## INSTRUCTIONS

- (1) After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- (2) This paper consists of TWO sections, A and B.
- (3) Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- (4) Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- (5) Unless otherwise specified, all working must be clearly shown.
- (6) Unless otherwise specified, numerical answers should be either exact or given to 4 decimal places.
- (7) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

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Candidate Number



1. The table below shows the probability distribution of a discrete random variable X, where a is a constant and p > 0.

x	0	1	2
P(X = x)	1 – 4 p	ар	р

(a) Find a.

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(b) If  $Var(2X + a^2) = 8E(aX - 1)$ , find p.

(6 marks)

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		ocopier $X$ , the probability that there is dirt on a page of photocopy is $\frac{1}{5}$ . A documer is photocopied repeatedly by using $X$ .
(a)	Find	the probability that there is dirt on a photocopy of the document.
(b)	A ph the p	notocopy of the document is called <i>acceptable</i> if there is dirt on fewer than 3 pages, otherwis thotocopy is called <i>unacceptable</i> .
	(i)	Find the probability that a photocopy of the document is unacceptable.
	(ii)	If an <i>unacceptable</i> photocopy of the document is just produced, find the expected number of acceptable photocopies produced between this <i>unacceptable</i> photocopy and the next <i>unacceptable</i> photocopy.
		(6 marks)
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them	ribe next year. It is given that the publisher randomly selects 841 current subscribers, and 441 current subscribers, and 441 current subscribers.
(a)	Find an approximate 95% confidence interval for $p$ .
(b)	An approximate $\beta\%$ confidence interval for $p$ is now constructed. The width of the confidence
	interval is 0.088. Find $\beta$ correct to the nearest integer. (6 marks
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( )	
(a)	Express, in terms of $k$ , the constant term and the coefficient of $x^2$ in the expansion of $f(x)$ .
(b)	If the constant term in the expansion of $f(x)$ is 27, find the coefficient of $x^2$ in this expansion (6 mag)
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Defir	e $g(x) = x + \frac{3}{x} + \ln x^4$ for all non-zero real numbers x.
(a)	Find $g'(x)$ .
(b)	Someone claims that the maximum value of $g(x)$ is less than the minimum value of $g(x)$ Do you agree? Explain your answer.
(c)	Write down the equations of the two horizontal tangents to the graph of $y = g(x)$ . (6 marks)
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(a)	Let $V  \mathrm{cm}^3$ and $r  \mathrm{cm}$ be the volume and the base radius of the circular cylinder respectively Find $\frac{\mathrm{d} V}{\mathrm{d} r}$ .
(b)	Can the volume of the circular cylinder exceed 5000 cm <sup>3</sup> ? Explain your answer. (6 mark
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Let n	n be a non-zero constant.
(a)	By considering $\frac{\mathrm{d}}{\mathrm{d}x}(xe^{mx})$ , find $\int xe^{mx}\mathrm{d}x$ .
(b)	If the area of the region bounded by the curve $y = xe^{mx}$ , the x-axis and the straight line $x = \frac{1}{m}$ , find $m$ .
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	SECT	TION E	3 (50 n	narks)
	9.	depar with a	ting bu a mean	ng Tom leaves home at 7:10 and walks to a certain bus stop to catch bus. He catches the earliest is when he arrives at the bus stop. The time taken for Tom's walk follows a normal distribution of 15 minutes and a standard deviation of 2 minutes. There are two buses each morning, 7:23 and 7:30 respectively.
		(a)	Find	the probability that Tom catches the bus departing at 7:23 on a certain morning. (2 marks)
		(b)	Find	the probability that Tom catches the bus departing at 7:30 on a certain morning. (1 mark)
ŧ		(c)	earlie catche	morning Mary, Tom's student, walks to the same bus stop to catch bus. She catches the set departing bus when she arrives at the bus stop. It is given that the probability that Mary es the bus departing at 7:23 on a certain morning is 0.3015, while the probability that she es the bus departing at 7:30 on a certain morning is 0.6328. If Mary and Tom catch the same Mary will greet Tom.
			(i)	Find the probability that the 4th day in a week is the 2nd time Mary greets Tom.
ked.			(ii)	Given that Mary greets Tom on 2 certain mornings, find the probability that Mary and Tom catch the bus departing at 7:30 on these 2 mornings.
ot be mar			(iii)	Given that Mary greets Tom on 4 certain mornings, find the probability that Mary and Tom catch the bus departing at 7:23 on at least 1 of these 4 mornings.
gins will no			(iv)	If Tom wants to have a higher chance of catching the bus departing at 7:23 than that of Mary, what is the latest time for him to leave home? Give your answer correct to the nearest minute.  (10 marks)
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10. A shopping mall launches a campaign to celebrate its fifth anniversary of the opening. A customer can throw a fair die 4 times to receive cash coupons. For each throw, a cash coupon is awarded according to the following table:

Result	1, 2 or 3	4 or 6	5
Value of cash coupon	\$10	\$25	\$50

(a) Find the probability that a customer receives cash coupons of a total value \$200.

(1 mark)

(b) Find the probability that a customer receives cash coupons of a total value not less than \$150.

(2 marks)

(c) A customer who receives cash coupons of a total value not less than \$150 can join a game. In the game, the customer presses a button 3 times. A number of cakes will show up on a screen for each press of the button, and the number of cakes shown follows a Poisson distribution with a mean of 5. The result of each press of button is classified as follows:

Number of cakes	1 to 4	5	otherwise
Result	Good	Excellent	Fair

The customer receives a prize according to the following results:

Result	1 Excellent and 2 Good	2 Excellent and 1 Good	3 Excellent
Prize	a cup	a backpack	an oven

- (i) Find the probability that a customer joining the game receives a backpack.
- (ii) Given that a customer joining the game receives a prize, find the probability that the customer receives an oven.
- (iii) A customer who cannot join the game can still receive a cup by joining a lucky draw. In the lucky draw, the probability of receiving a cup is 0.01. Given that a customer receives a cup, find the probability that the customer cannot join the game.

(9 marks)

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$$A(t) = 5\ln(t^2 - 8t + 20) ,$$

where t is the number of months elapsed since the park opens. Denote the total number of adults visiting the park in the first 2 months since the park opens by  $\alpha$  thousand. Let  $\alpha_1$  be the estimate of  $\alpha$  by using the trapezoidal rule with 5 sub-intervals.

- (a) (i) Find  $\alpha_1$ .
  - (ii) Is  $\alpha_1$  an over-estimate or an under-estimate? Explain your answer.

(5 marks)

(b) The manager models the rate of change of the number of children (in thousand per month) visiting the park by

$$B(t) = \frac{3^{2t+2}}{1+3^{2t}} ,$$

where t is the number of months elapsed since the park opens.

- (i) Find the total number of children visiting the park in the first 2 months since the park opens.
- (ii) The manager claims that in the first 2 months since the park opens, the difference of the total number of adults visiting the park and the total number of children visiting the park exceeds 40% of the total number of adults visiting the park. Do you agree? Explain your answer.

(7 marks)

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$$P = \frac{32}{a^{5+bt} + 8} \ ,$$

where a and b are constants and t ( $t \ge 0$ ) is the number of months elapsed since the start of the study.

(a) Express  $\ln\left(\frac{32}{P} - 8\right)$  as a linear function of t.

(2 marks)

- (b) John finds that the graph of the linear function obtained in (a) passes through the point  $(1, \ln 2)$  and the intercept on the vertical axis of the graph is  $\ln 32$ .
  - (i) Find a and b.
  - (ii) Find  $\frac{dP}{dt}$  and  $\frac{d^2P}{dt^2}$ .
  - (iii) Estimate the number of ducks in the farm after a very long time. Hence, or otherwise, prove that the number of ducks in the farm does not exceed 4 thousand since the start of the study.
  - (iv) Find the number of ducks in the farm when  $\frac{dP}{dt}$  attains its greatest value.

(11 marks)

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Standard Normal Distribution Table

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0.7         2580         .2611         .2642         .2673         .2704         .2734         .2764         .2794         .2823         .2851           0.8         .2881         .2910         .2939         .2967         .2995         .3023         .3051         .3078         .3106         .3133           0.9         .3159         .3186         .3212         .3238         .3264         .3289         .3315         .3340         .3365         .3385           1.0         .3413         .3438         .3461         .3485         .3508         .3531         .3554         .3577         .3599         .3621           1.1         .3643         .3665         .3686         .3708         .3729         .3749         .3770         .3790         .3810         .3831           1.2         .3849         .3869         .3888         .3907         .3925         .3944         .3962         .3980         .3997         .4015           1.3         .4032         .4049         .4066         .4082         .4099         .4115         .4131         .4147         .4162         .4177           1.4         .4192         .42477         .4222         .4236         .4251         <	1	1						.2123	.2157		.2224
0.8         .2881         .2910         .2939         .2967         .2995         .3023         .3051         .3078         .3166         .3133           0.9         .3159         .3186         .3212         .3238         .3264         .3289         .3315         .3340         .3365         .3385           1.0         .3413         .3438         .3461         .3485         .3508         .3531         .3577         .3599         .3621           1.1         .3643         .3665         .3686         .3708         .3729         .3749         .3770         .3790         .3810         .3830           1.2         .3849         .3869         .3888         .3907         .3925         .3944         .3962         .3980         .3997         .4015           1.3         .4032         .4049         .4066         .4082         .4099         .4115         .4131         .4147         .4162         .4177           1.4         .4192         .4207         .4222         .4236         .4251         .4265         .4279         .4292         .4306         .4315           1.5         .4332         .4345         .4357         .4370         .4382         .4394         <	1	1							.2486	.2517	.2549
0.9         .3159         .3186         .3212         .3238         .3264         .3289         .3315         .3340         .3365         .3385           1.0         .3413         .3438         .3461         .3485         .3508         .3531         .3554         .3577         .3599         .3621           1.1         .3643         .3665         .3686         .3708         .3729         .3749         .3770         .3790         .3810         .3831           1.2         .3849         .3869         .3888         .3907         .3925         .3944         .3962         .3980         .3997         .4015           1.3         .4032         .4049         .4066         .4082         .4099         .4115         .4131         .4147         .4162         .4177           1.4         .4192         .4207         .4222         .4236         .4251         .4265         .4279         .4292         .4306         .4315           1.5         .4332         .4345         .4357         .4370         .4382         .4394         .4406         .4418         .4429         .4441           1.6         .4452         .4463         .4474         .4484         .4495         <	1						.2734	.2764	.2794	.2823	.2852
1.0         .3413         .3438         .3461         .3485         .3508         .3531         .3554         .3577         .3599         .3621           1.1         .3643         .3665         .3686         .3708         .3729         .3749         .3770         .3890         .3890         .3830           1.2         .3849         .3869         .3888         .3907         .3925         .3944         .3962         .3980         .3997         .4015           1.3         .4032         .4049         .4066         .4082         .4099         .4115         .4131         .4147         .4162         .4177           1.4         .4192         .4207         .4222         .4236         .4251         .4265         .4279         .4292         .4306         .4319           1.5         .4332         .4345         .4357         .4370         .4382         .4394         .4406         .4418         .4429         .4441           1.6         .4452         .4463         .4474         .4484         .4495         .4505         .4515         .4525         .4535         .4545           1.7         .4554         .4564         .4573         .4582         .4591         <		1				.2995	.3023	.3051	.3078	.3106	.3133
1.1       .3643       .3665       .3686       .3708       .3729       .3749       .3770       .3790       .3810       .3831         1.2       .3849       .3869       .3888       .3907       .3925       .3944       .3962       .3980       .3997       .4015         1.3       .4032       .4049       .4066       .4082       .4099       .4115       .4131       .4147       .4162       .4177         1.4       .4192       .4207       .4222       .4236       .4251       .4265       .4279       .4292       .4306       .4319         1.5       .4332       .4345       .4357       .4370       .4382       .4394       .4406       .4418       .4429       .4441         1.6       .4452       .4463       .4474       .4484       .4495       .4505       .4515       .4525       .4535       .4545         1.7       .4554       .4564       .4573       .4582       .4591       .4599       .4608       .4616       .4625       .4633         1.8       .4641       .4649       .4656       .4664       .4671       .4678       .4686       .4693       .4699       .4706         2.0       .4772	0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.2       3849       .3869       .3888       .3907       .3925       .3944       .3962       .3980       .3997       .4015         1.3       .4032       .4049       .4066       .4082       .4099       .4115       .4131       .4147       .4162       .4177         1.4       .4192       .4207       .4222       .4236       .4251       .4265       .4279       .4292       .4306       .4319         1.5       .4332       .4345       .4357       .4370       .4382       .4394       .4406       .4418       .4429       .4441         1.6       .4452       .4463       .4474       .4484       .4495       .4505       .4515       .4525       .4535       .4545         1.7       .4554       .4564       .4573       .4582       .4591       .4599       .4608       .4616       .4625       .4633         1.8       .4641       .4649       .4656       .4664       .4671       .4678       .4686       .4693       .4699       .4706         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821	1	1									.3621
1.3       .4032       .4049       .4066       .4082       .4099       .4115       .4131       .4147       .4162       .4177         1.4       .4192       .4207       .4222       .4236       .4251       .4265       .4279       .4292       .4306       .4319         1.5       .4332       .4345       .4357       .4370       .4382       .4394       .4406       .4418       .4429       .4441         1.6       .4452       .4463       .4474       .4484       .4495       .4505       .4515       .4525       .4535       .4545         1.7       .4554       .4564       .4573       .4582       .4591       .4599       .4608       .4616       .4625       .4633         1.8       .4641       .4649       .4656       .4664       .4671       .4678       .4686       .4693       .4699       .4706         1.9       .4713       .4719       .4726       .4732       .4738       .4744       .4750       .4756       .4761       .4767         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821		1									.3830
1.4       .4192       .4207       .4222       .4236       .4251       .4265       .4279       .4292       .4306       .4315         1.5       .4332       .4345       .4357       .4370       .4382       .4394       .4406       .4418       .4429       .4441         1.6       .4452       .4463       .4474       .4484       .4495       .4505       .4515       .4525       .4535       .4545         1.7       .4554       .4564       .4573       .4582       .4591       .4599       .4608       .4616       .4625       .4633         1.8       .4641       .4664       .4651       .4678       .4686       .4693       .4699       .4706         1.9       .4713       .4719       .4726       .4732       .4738       .4744       .4750       .4756       .4761       .4767         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4857       .4857         2.2       .4861       .4864       .4868       .4871										.3997	.4015
1.5       .4332       .4345       .4357       .4370       .4382       .4394       .4406       .4418       .4429       .4441         1.6       .4452       .4463       .4474       .4484       .4495       .4505       .4515       .4525       .4535       .4545         1.7       .4554       .4564       .4573       .4582       .4591       .4599       .4608       .4616       .4625       .4633         1.8       .4641       .4649       .4656       .4664       .4671       .4678       .4686       .4693       .4699       .4706         1.9       .4713       .4719       .4726       .4732       .4738       .4744       .4750       .4756       .4761       .4767         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4887       .4890         2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4884       .4887       .4890         2.3       .4893       .4896	1								.4147	.4162	.4177
1.6       .4452       .4463       .4474       .4484       .4495       .4505       .4515       .4525       .4535       .4545         1.7       .4554       .4564       .4573       .4582       .4591       .4599       .4608       .4616       .4625       .4633         1.8       .4641       .4649       .4656       .4664       .4671       .4678       .4686       .4693       .4699       .4706         1.9       .4713       .4719       .4726       .4732       .4738       .4744       .4750       .4756       .4761       .4767         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4857       .4857         2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4884       .4887       .4890         2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920	1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.7       .4554       .4564       .4573       .4582       .4591       .4599       .4608       .4616       .4625       .4633         1.8       .4641       .4649       .4656       .4664       .4671       .4678       .4686       .4693       .4699       .4706         1.9       .4713       .4719       .4726       .4732       .4738       .4744       .4750       .4756       .4761       .4767         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4850       .4857       .4878       .4881       .4884       .4887       .4890         2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4884       .4887       .4890         2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934 <td>1</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>.4441</td>	1										.4441
1.8       .4641       .4649       .4656       .4664       .4671       .4678       .4686       .4693       .4699       .4706         1.9       .4713       .4719       .4726       .4732       .4738       .4744       .4750       .4756       .4761       .4767         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4850       .4854       .4857         2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4884       .4887       .4890         2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934       .4936         2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953											
1.9       .4713       .4719       .4726       .4732       .4738       .4744       .4750       .4756       .4761       .4767         2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4850       .4854       .4857         2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4884       .4887       .4890         2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934       .4936         2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965		1									
2.0       .4772       .4778       .4783       .4788       .4793       .4798       .4803       .4808       .4812       .4817         2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4850       .4854       .4857         2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4844       .4887       .4890         2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934       .4936         2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974											
2.1       .4821       .4826       .4830       .4834       .4838       .4842       .4846       .4850       .4854       .4857         2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4884       .4887       .4890         2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934       .4936         2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974       .4982       .4983       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988		1	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.2       .4861       .4864       .4868       .4871       .4875       .4878       .4881       .4884       .4887       .4890         2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934       .4936         2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974       .4975       .4976       .4977       .4977       .4978       .4979       .4979       .4980       .4981         2.9       .4981       .4982       .4982       .4983       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987		1			.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.3       .4893       .4896       .4898       .4901       .4904       .4906       .4909       .4911       .4913       .4916         2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934       .4936         2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974       .4975       .4976       .4977       .4977       .4978       .4979       .4979       .4980       .4981         2.9       .4981       .4982       .4983       .4984       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4992       .4992       .4992       .4992       .4993       .4993         3.2	1		.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.4       .4918       .4920       .4922       .4925       .4927       .4929       .4931       .4932       .4934       .4936         2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974       .4975       .4976       .4977       .4977       .4978       .4979       .4979       .4980       .4981         2.9       .4981       .4982       .4983       .4984       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4990       .4990         3.1       .4990       .4991       .4991       .4991       .4992       .4992       .4992       .4992       .4993       .4993         3.2       .4993       .4995       .4995       .4996		1	.4864			.4875	.4878	.4881	.4884	.4887	.4890
2.5       .4938       .4940       .4941       .4943       .4945       .4946       .4948       .4949       .4951       .4952         2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974       .4975       .4976       .4977       .4978       .4979       .4979       .4980       .4981         2.9       .4981       .4982       .4983       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4989       .4990       .4990         3.1       .4990       .4991       .4991       .4992       .4992       .4992       .4992       .4993       .4993         3.2       .4993       .4995       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996	•	1				.4904	.4906	.4909	.4911	.4913	.4916
2.6       .4953       .4955       .4956       .4957       .4959       .4960       .4961       .4962       .4963       .4964         2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974       .4975       .4976       .4977       .4977       .4978       .4979       .4979       .4980       .4981         2.9       .4981       .4982       .4982       .4983       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4990       .4990         3.1       .4990       .4991       .4991       .4991       .4992       .4992       .4992       .4993       .4993         3.2       .4993       .4993       .4994       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997 <td>2.4</td> <td>.4918</td> <td>.4920</td> <td>.4922</td> <td>.4925</td> <td>.4927</td> <td>.4929</td> <td>.4931</td> <td>.4932</td> <td>.4934</td> <td>.4936</td>	2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.7       .4965       .4966       .4967       .4968       .4969       .4970       .4971       .4972       .4973       .4974         2.8       .4974       .4975       .4976       .4977       .4977       .4978       .4979       .4979       .4980       .4981         2.9       .4981       .4982       .4983       .4984       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4990       .4990         3.1       .4990       .4991       .4991       .4992       .4992       .4992       .4992       .4993       .4993         3.2       .4993       .4993       .4994       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996       .4996       .4997       .499		1									.4952
2.8       .4974       .4975       .4976       .4977       .4977       .4978       .4979       .4979       .4980       .4981         2.9       .4981       .4982       .4982       .4983       .4984       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4989       .4990       .4990         3.1       .4990       .4991       .4991       .4991       .4992       .4992       .4992       .4993       .4993         3.2       .4993       .4993       .4994       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996       .4996       .4996       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4998		1									VII. 2005CPXCD201
2.9       .4981       .4982       .4982       .4983       .4984       .4984       .4985       .4985       .4986       .4986         3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4989       .4990       .4990         3.1       .4990       .4991       .4991       .4992       .4992       .4992       .4992       .4993       .4993         3.2       .4993       .4993       .4994       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996       .4996       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4998		1						.4971			.4974
3.0       .4987       .4987       .4988       .4988       .4989       .4989       .4989       .4990       .4990         3.1       .4990       .4991       .4991       .4992       .4992       .4992       .4992       .4993       .4993       .4993         3.2       .4993       .4993       .4994       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996       .4996       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4998		1							.4979	.4980	.4981
3.1       .4990       .4991       .4991       .4992       .4992       .4992       .4992       .4993       .4993       .4993         3.2       .4993       .4993       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996       .4996       .4996       .4997         3.4       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4998		.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.2       .4993       .4993       .4994       .4994       .4994       .4994       .4994       .4995       .4995       .4995         3.3       .4995       .4995       .4996       .4996       .4996       .4996       .4996       .4996       .4996       .4996       .4997         3.4       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4997       .4998											202 2020 2020 0000 0
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3.5   .4998   .4998   .4998   .4998   .4998   .4998   .4998   .4998   .4998   .4998	3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
	3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note: An entry in the table is the area under the standard normal curve between x = 0 and x = z  $(z \ge 0)$ . Areas for negative values of z can be obtained by symmetry.

